## Unit 4 Study Guide

Convert the equation to logarithmic form: $42=x^{3}$

Convert the equation into exponential form: $\log _{64} 16=\frac{2}{3}$

Evaluate:

| $\log _{64} 8$ | $\log _{16} \frac{1}{2}$ | $\log _{17} 17$ | $\log _{4}-8$ |
| :--- | :--- | :--- | :--- |
| $\log _{3} \frac{1}{81}$ | $9^{\log _{9} 81}$ | $\log _{5} 27$ | $e^{\ln 6}$ |
| $\ln \cdot e^{32}$ | $\frac{\ln \cdot e^{6}}{18}$ | $3.5 e^{4}$ | $e^{5}$ |

Condense:

| $\log _{3} x+\log _{3} x$ | $2 \log _{4} x+\log _{4}(x+2)$ | $\log _{5}(x+1)+\log _{3}(x+2)$ |
| :---: | :---: | :---: |
| $\log \left(x^{2}-4\right)-\log (x+2)$ | $\ln 4 x+3 \ln x$ | $3 \ln x-2 \ln x$ |
|  |  |  |

Expand:

| $\log _{2} 5 x^{2}$ | $\log \frac{5 x}{y}$ | $\log \sqrt{\frac{m}{n}}$ |
| :---: | :---: | :---: |
| $\log 2 x^{3} y$ | $\ln x^{3} y^{2}$ | $\ln \sqrt[3]{m n}$ |

Solve the following Exponential Equations:

| $4^{3}=2^{x}$ | $3^{5 x-6}=81$ | $3^{x-11}=7$ |
| :---: | :---: | :---: |

Solve the following Logarithmic Equations:

| $\log _{3}(4 x-3)=4$ | $\log (2 x+6)=\log \left(2 x^{2}+7 x-6\right)$ | $\log x-\log 9=\log 18$ |
| :---: | :---: | :---: |
| $\log (x+3)+\log (x+4)=\log x+\log (x+8)$ | $\log (3 x+7)=3$ |  |
|  |  |  |

Solve the following Equations:

| $4 e^{x}-3=6$ | $e^{3} \cdot e^{x}=15$ |
| :--- | :---: |
| $\ln (3 x+4)=9$ | $\ln 4 x+\ln 2 x=8$ |
|  |  |

## Exponential Growth/Decay

1.) Determine if the following functions are grow or decay.
2.) Determine the growth or decay factor as a percent.

| $f(x)=6(1.04)^{x}$ | $f(x)=11(.86)^{x}$ |
| :--- | :--- |
|  |  |

In 2010, there was a population 2165 mice and they are decreasing at a rate of $17 \%$ per year.
a. Write an exponential function for this model.
b. Predict how many mice there will be this year.
c. When will there be 1200 mice?

Iron-59 is used in medicine to diagnose blood circulation disorders. The half-life of iron-59 is 44.5 days.
a. Write an exponential function that models the decay of this substance?
b. How much of a 2.0 mg sample will remain after 133.5 days?
c. How long will it take to have a 2.5 mg of iron-59 left over?

You saved \$2500 from your summer job. Which option yields more money? What is the positive difference between the 2 options?

Option 1:
A traditional savings account at $3.5 \%$ interest compounded monthly for 5 years.

Find the inverse of the following function:
$f(x)=\log _{5}(x-2)+4$
$f(x)=3^{x+3}-5$

Graph:


